

2.3 Linear Functions

Slopes of Lines

The slope of a line is a measure of the steepness of a line. Slope = m .

The slope of a line containing two points

is the ratio of the change in y -coordinate to the change in x -coordinates.

The Slope Formula to find the slope between two points (x_1, y_1) and (x_2, y_2) is:

$$m = \frac{\text{rise}}{\text{run}} = \frac{\text{change in } y}{\text{change in } x} = \frac{y_2 - y_1}{x_2 - x_1}$$

Examples: Find slope between the given points.

1. $(4, -1)$ and $(-1, 3)$
2. $(1, 5)$ and $(3, 5)$

Finding the Equation of a Line

If given a point, (x_1, y_1) and the slope, m , then the equation can be written in

$$\text{Point-Slope Form: } y - y_1 = m(x - x_1)$$

If given two points on the line, first find the slope between the two points. Then use the same method for a given point and slope.

Examples:

Find an equation of the line that contains the given point and slope:

1. Point $(2, 4)$, $m = 3$
2. Point $(2, 3)$, $m = -\frac{1}{2}$

3. Point $(-5,-1)$, $m = \text{undefined}$

4. $P_1 = (1,2)$ $P_2 = (2,4)$

Slope-Intercept Form

The equation of a line can be written in the form $y = mx + b$, when the y-intercept and the slope of the line are given.

When an equation is in the form $y = mx + b$, the slope = m , the y-intercept = b or $(0, b)$.

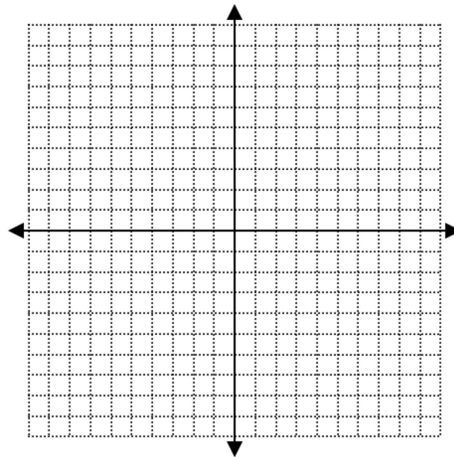
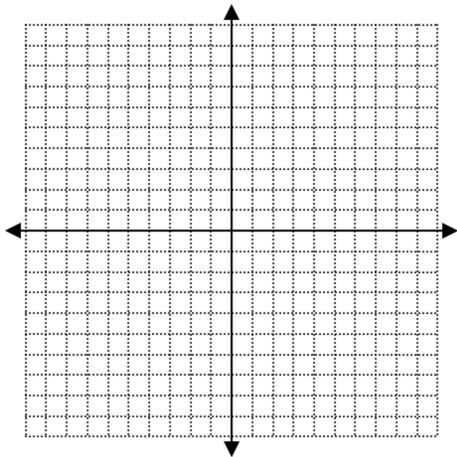
The line can be graphed by plotting the y-intercept and then using the slope to find additional points on the graph. Draw a line through the points, across the graph.

Be sure the equation is in $y = mx + b$ form first

Examples:

1. Graph $y = -\frac{2}{3}x - 2$

2. Graph $-2x + y = -3$



Parallel and perpendicular lines

Two lines that have that do not intersect are called *parallel lines*. Parallel lines have the same slope.

Two lines that intersect at right angles are called *perpendicular lines*. Their slopes are opposite reciprocals (a/b and $-b/a$). If $m_1 \cdot m_2 = -1$, then the slopes are perpendicular.

Examples:

1. Determine if the line that contains the points $(-2,3)$ and $(5,-2)$ and the line that contains the points $(2,4)$ and $(-3,-3)$ are perpendicular, parallel, or neither.

2. Are the lines $2x - 4y = 3$ and $2x + 4y = -3$ parallel?

3. Find the equation of the line containing the point $(2,1)$ and is parallel to the line $3x + y = -1$.

4. Find the equation of the line containing the point $(1,-2)$ and is perpendicular to the line $y = \frac{3}{2}x - 2$